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## Vibration Analysis of a Cantilever beam with Crack depth and Crack Location Effects

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Aluminum Alloy, Copper Alloy, Titanium Alloy, Natural frequency Mode Shapes

## Abstract

Alloy beams and beam like elements are principal constituents of many structures and widely used in high speed machinery, aircraft and light weight structures. Crack is a damage that often occurs on members of structures and may cause serious failures of structures. In this research the natural frequency of a cracked cantilever beam is investigated by finite element method by using of ANSYS program with different crack depth and location effect.

The beam material studied is aluminum alloy, titanium alloy, copper alloy and magnesium alloy. A comparison is made between these alloys and conclude optimized result between them. The increase of the beam length result in a decrease in the natural frequencies of the composite beam and also shows that an increase of the depth of cracks lead to a decrease in the value of natural frequencies.

## 1. Introduction

All structures are subjected to degenerative effects that may cause initiation of structural defects such as cracks which, as time progresses, lead to the catastrophic failure or breakdown of the structure. Thus, the importance of inspection in the quality assurance of manufactured products is well understood. Cracks or other defects in a structural element influence its dynamical behavior and change its stiffness and damping properties. Consequently, the natural frequencies of the structure contain information about the location and dimensions of the damage [1].

The dynamic response-based damage detection method attracts most attention due to its simplicity for implementation. This technique makes use of the dynamic response of structures which offers unique information on the defects contained with these structures. Changes in the physical properties of the structures due to damage can alter the dynamic response, such as the natural frequency and mode shape. These parameter changes can be extracted to predict damage detection information, such as the presence, location, and severity of damage in a structure. The natural frequency provides the simplest damage detection method since damage tends to reduce the stiffness of the structure. Therefore, a reduction of natural frequency may indicate the existence of damage in the structure. However, the natural frequency is a global feature of the structure, from which the location of the damage is difficult to determine. The modal parameters (e.g., the mode shape and flexibility), which can capture the local perturbation due to damage are used in order to locate damage [2].

A crack may reduce the flexural rigidity of a column and its load carrying capacity .From the reduced flexural rigidity, the deflection and the load carrying capacity of a notched column may be calculated .The bending at the crack section of a column causes a tensile mode crack up stress field, which is characterized by a stress intensity factor. When the stress intensity factor at a crack tip exceeds the fracture toughness of the material, fracture occurs. The fracture toughness of cracked column is studied [3].

In many circumstances material flaws are present in

Husain Mehdi husainmehdi4u7@gmail.com Copyright ©ijrei.com structures made of anisotropic composites .Such cracks can be detected by vibrational analysis based on the variation of the local compliance as the crack gradually grows. The significance of this term on the local flexibility of a centrally cracked plate is discussed by presenting a numerical example for a graphite fiber for a reinforced polyamide composite. The prospect of crack diagnosis of composite components on the basis of coupled deformation modes due to the crack presence is signified by analyzing the compliance matrix of a prismatic beam containing a central crack [4].

A crack in a structural element introduces a significant local flexibility which enhances the instability. Buckling of a edge notched beam is studied for isotropic and anisotropic composites. The local compliance due to presence of cracks in anisotropic medium is formulated as a function of crack -tip stress intensity factors and the elastic constants of the material [5].

The equation of motion & associated boundary conditions are derived for a uniform Bernoulli-Euller beam containing one single- edge crack. The main idea is to use a generalized vibrational principle that allows for modified stress, strain, & displacement field that enable one to satisfy the compatibility requirements in the vicinity of the crack [6].

It was investigated a new beam finite element with a single non-propagating one-edge open crack located in its midlength is formulated for the static & dynamic analysis of cracked composite beam -like structures. The element include two degree of freedom at each of the three nodes, a transverse deflection and an independent rotation respectively [7].

The Eigen frequencies of a cantilever beam, made from graphite fiber reinforced polyamide with a transverse one edge non-propagating open crack are investigated .Two models of beam are presented.in the first model the crack is modelled by a massless substitute spring .The flexibility of the spring is calculated on the basis of fracture mechanics and the castigiliano theorem. The second model is based on the finite element method (FEM) [8].

It was investigated that the presence of a crack in a structural member introduces a local flexibility that effects its vibration response .Moreover the crack will open and close in time depending on the rotation and vibration amplitude .In this case the system is non-linear [9].

The characteristic matrices of a composite beam with single transverse fatigue crack are presented. The element developed has been applied in analyzing influence of the cracked parameters (position and relative depth)and the material parameters relative volume and fiber angle)on changes in the first four transverse natural frequencies of the composite beam made to unidirectional composite material [10].

The dynamics of a fixed-three bar with a breathing crack in longitudinal vibration is investigated .The crack was modelled as a continuous flexibility using the displacement field in the vicinity of the crack found with fracture mechanics methods[11].

It was investigated that a piece-wise linear approach to analyze vibrations of a cantilever beam with a 'breathing crack'. Their formulation was hybrid frequencydomain/time-domain method. For the majority of vibration, the crack section is unambiguously either open or closed [12]. The numerical modelling of damage and crack propagation in concrete and concrete structures has evolved considerably in the past years. In this contribution ,a higher order continuum model is used to model the failure behavior of single -edge notched & double- edge notched concrete beams loaded in four-point shear .The influence of the ratio of the compressive strength & the tensile strength is scrutinized and its relation with the failure mechanism is investigated [13].

It was analyzed that the dynamic behavior of cracked beam, the effect of crack on a structure by comparing the signal in frequency & the time domain: and concluded that ,increase in crack depth results the increase in amplitude of vibration .Secondly the amplitude of low frequency vibration decreases and high frequency vibration increases when the location of crack increases [14].

The modelling methods of structural elements with failures (cracks and delamination) is presented. Cracks appear in both isotropic and anisotropic materials .Delamination is one of the most important failure modes of laminated composite materials. Delamination may originate during manufacturing or may be induced during in -service loading ,such as by foreign object impact or by fatigue common damage in composite materials is matrixcracking, fiber-breakage ,fiber-matrix debounding [15]. different approaches to crack modelling , and demonstrates that for structural health monitoring using low frequency vibration based on beam elements are adequate .They also addresses the effect of the excitation of breathing cracks, where the beam stiffness is bilinear ,depending upon the whether the beam is open or close [16].

The bending free vibration of cantilevered composite beams weakened by multiple non-propagating part through surface crack is presented .Toward determining the local flexibility characteristics induced by the individual cracks, the concept of massless rotation is applied [17].

## 2. Governing Equation

## 2.1 Structure Analysis

The differential equation of the bending of a beam with a mid-plane symmetry (Bij = 0) so that there is no bending-stretching coupling and no transverse shear deformation (xz=0) is given by

$$IS_{11}(d^4\omega/d\omega^4) = q(x)$$
(1)

It can easily be shown that under these conditions if the beam involves only a one layer, isotropic material, then  $IS_{11}=EI=Ebh^3/12$  and for a beam of rectangular cross-section Poisson's ratio effects are ignored in beam theory, which is in the line with Vinson & Sierakowski (1991).

In Equation 1, it is seen that the imposed static load is

written as a force per unit length. For dynamic loading, if Alembert's Principle are used then one can add a term to Equation.1 equal to the product mass and acceleration per unit length. In that case Equation.1 becomes

$$IS_{11}d^4\omega(x,t)/d\omega^4 = q(x,t) - \rho F \partial^2 \omega(x,t)/\partial x^2$$
(2)

where and q both become functions of time as well as space, and derivatives therefore become partial derivatives,

is the mass density of the beam material, and here F is the beam cross- sectional area. In the above, q(x, t) is now the spatially varying time-dependent forcing function causing the dynamic response, and could be anything from a harmonic oscillation to an intense one-time impact.

For a composite beam in which different lamina have differing mass densities, then in the above equations use, for a beam of rectangular cross-section

$$\rho F = \rho bh = \sum_{k=1}^{N} \rho b(h_k - h_{k-1}) \tag{3}$$

However, natural frequencies for the beam occur as functions of the material properties and the geometry and hence are not affected by the forcing functions; therefore, for this study let q(x,t) be zero.

Thus, the natural vibration equation of a mid-plane symmetrical composite beam is given by

$$IS_{11}[d4\omega(x,t)/d\omega^4] + \rho F[\partial^2 \omega(x,t)/\partial x^2] = 0$$
(4)

It is handy to know the natural frequencies of beams for various practical boundary conditions

In order to insure that no recurring forcing functions are close to any of the natural frequencies, because that would result almost certainly in a structural failure. In each case below, the natural frequency in radians /unit time is given as

$$\omega_{\rm n} = \alpha^2 \sqrt{(IS_{11}/\rho F L^4)} \tag{5}$$

Where <sup>2</sup> is the co-efficient, which value is catalogued by Warburton, Young and Felgar and once <sub>n</sub> is known then the natural frequency in cycles per second (Hertz) is given by  $f_n = n/2$ , which is in the line with Vinson & Sierakowski (1991).

In general, governing equation for free vibration of the beam can be expressed as

$$[K]-\omega^{2}[M]{q}=0$$
(6)

Where, K = Stiffness matrix

M = Mass matrix, and q = degrees of freedom.

### 2.2 Modal Analysis (Mehdi. H et al [24])

## 2.2.1 Damping Matrices

Damping may be introduced into a transient, harmonic, or damped modal analysis as well as a response spectrum. The type of damping allowed depends on the analysis as described in the subsequent sections.

Transient (Full or Reduced) Analysis and Damped Modal Analysis:

The damping matrix, [C], may be used in transient and damped modal analyses as well as substructure generation. In its most general form, the damping matrix is composed of the following components.

$$[C] = r[M] + (s + \frac{2}{\Omega}g)[K] + \sum_{i=1}^{N_{ac}} r_i^{m}[M_i] + \sum_{j=1}^{N_{ac}} [(s_j^{m} + \frac{2}{\Omega}g_j + \frac{1}{\Omega}g_j^{E})[K_j]] + \sum_{k=1}^{N_{ac}} [C_k] + \sum_{m=1}^{N_{ac}} \frac{1}{\Omega} [C_m] + \sum_{l=1}^{N_{ac}} [G_l]$$

$$(7)$$

Where

[C] = structure damping matrix, = mass matrix multiplier, [M] = structure mass matrix, = stiffness matrix multiplier, [K] = structure stiffness matrix, Nma = number of materials, im = mass matrix multiplier for material I, [Mi] = portion of structure mass matrix based on material I, Nmb

= number of materials,  $S_j^m$  = stiffness matrix multiplier for material j, [Kj] = portion of structure stiffness matrix based on material j, Ne = number of elements with specified damping, , [Ck] = element damping matrix, Ng = number of elements with Coriolis or gyroscopic damping, [Gl] = element Coriolis or gyroscopic damping matrix Harmonic (Full or Reduced) Analysis:

The damping matrix ([C]) used in harmonic analyses is composed of the following components.

$$\begin{bmatrix} \mathbf{C} \end{bmatrix} = \mathbf{\Gamma} \begin{bmatrix} \mathbf{M} \end{bmatrix} + (\mathbf{S} + \frac{2}{\Omega} \mathbf{g}) \begin{bmatrix} \mathbf{K} \end{bmatrix} + \sum_{i=1}^{N_{max}} \mathbf{\Gamma}_{i}^{m} \begin{bmatrix} \mathbf{M}_{i} \end{bmatrix} + \sum_{j=1}^{N_{max}} \begin{bmatrix} (\mathbf{S}_{j}^{m} + \frac{2}{\Omega} \mathbf{g}_{j} + \frac{1}{\Omega} \mathbf{g}_{j}^{E}) \begin{bmatrix} \mathbf{K}_{j} \end{bmatrix} \end{bmatrix} + \sum_{k=1}^{N_{x}} \begin{bmatrix} \mathbf{C}_{k} \end{bmatrix} + \sum_{m=1}^{N_{y}} \frac{1}{\Omega} \begin{bmatrix} \mathbf{C}_{m} \end{bmatrix} + \sum_{l=1}^{N_{g}} \begin{bmatrix} \mathbf{G}_{l} \end{bmatrix}$$

(8)

The input exciting frequency, , is defined in the range between  $_{\rm B}$  and  $_{\rm E}$  via

$$\begin{array}{l} _{B}=2 \ f_{B}, \\ _{E}=2 \ f_{E} \\ f_{B}= beginning \ frequency \\ f_{E}= end \ frequency \end{array}$$

Substituting equation (8) into the harmonic response equation of motion and rearranging terms yields

$$\begin{split} & [[K] + i \left\{ 2g[K] + \sum (2g_j + g_j^{E})[K_j] + \sum [C_m] \right\} + i\Omega[r[M] + \sum r_i^{m}[M_i] + S[K] + \\ & \sum s_j^{m}[K_j] + \sum [C_k] + \sum [G_j]](u_1 + iu_2) = F_1 - \Omega^2[M] \end{split}$$

(9)

The complex stiffness matrix in the first row of the equation consists of the normal stiffness matrix augmented by the structural damping terms given by g, g<sub>i</sub>, g<sub>i</sub><sup>E</sup>, and [C<sub>m</sub>] which produce an imaginary contribution. Structural damping is independent of the forcing frequency, , and produces a damping force proportional to displacement (or strain). The terms g, g<sub>i</sub>, and g<sub>i</sub><sup>E</sup> are damping ratios (i.e., the ratio between actual damping and critical damping, not to be confused with modal damping).

The second row consists of the usual viscous damping terms and is linearly dependent on the forcing frequency, , and produces forces proportional to velocity.

#### 2.2.2 **Mode-Superposition Analysis**

The damping matrix is not explicitly computed, but rather the damping is defined directly in terms of a damping ratio d. The damping ratio is the ratio between actual damping

ı d and critical damping. The damping ratio i for mode i is the combination of

$${}^{\prime}{}_{i}{}^{d} = {}^{\prime}{} + {}^{\prime}{}_{i}{}^{m} + \frac{\Gamma}{2\check{S}_{i}} + \frac{S}{2}\check{S}_{i}$$
(10)

Where

= constant modal damping ratio,  $i_{i}^{m}$  = modal damping ratio for mode shape i (see below), i = circular natural frequency associated with mode shape i = 2  $f_{i}$ ,  $f_{i}$  = natural frequency associated with mode shape I, = mass matrix multiplier

The modal damping ratio  $i_{i}^{m}$  can be defined for each mode directly (undamped modal analyses only).

Alternatively, for the case where multiple materials are present whose damping ratios are different, an effective mode-dependent damping ratio  $\int_{i}^{m}$  can be defined in the modal analysis if material-dependent damping is defined and the element results are calculated. This effective damping ratio is computed from the ratio of the strain energy in each material in each mode using

$${}'_{i}{}^{m} = \frac{\sum_{j=1}^{N_{m}} S^{m}{}_{j}E_{j}{}^{s}}{\sum_{j=1}^{N_{m}} E_{j}{}^{s}}$$
(11)

Where

 $N_m$  = number of materials,  $S_i^m$  = damping ratio for material j

$$E_{j}^{s} = \frac{1}{2} (\{_{i}\})^{\mathrm{T}} [\mathbf{K}_{j}] (\{ \})$$

Strain Energy contained in mode i for material j,  $\{i\}$  = displacement vector for mode I, [Kj] = stiffness matrix of part of structure of material j

(and material-dependent) These mode-dependent ratios,  $\zeta_i^m$  will be carried over into the subsequent modesuperposition or spectrum analysis. Note that any manually-defined damping ratios will overwrite those computed in the modal analysis via equation-11

## 3. Results and Discussions

In order to check the natural frequency of cantilever alloy beam, first we calculate the mechanical properties of Alalloy, Mg-alloy, Ti-alloy and Cu-alloy, like ultimate tensile strength, yielding strength.

In these alloys titanium alloy has a greater ultimate strength than the other alloys, whereas magnesium alloy has a lower ultimate strength.

These mechanical properties are fed into ANSYS-14.0 to calculate the natural frequency for alloy cantilever beam.

Table 1: Properties of Selected Materials

Material	Density Kg/m <sup>3</sup>	Tensile Yield Strength Mpa	Tensile Ultimate Strength Mpa
Mg- Alloy	1800	193	255
Al- Alloy	2770	280	310
Cu- Alloy	8300	280	430
Ti- Alloy	4620	930	1070









Figure 1: comparison of Mechanical properties (a) Tensile yield strength, (b) Ultimate tensile strength

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	50mm crack location				
Alloy	Natural Frequency (Hz)				
	Mode	without	2mm crack	4mm crack	
	Shape	crack	depth	depth	
	1	23.656	23.176	21.59	
	2	93.849	93.136	90.233	
Cu Alloy	3	147.97	144.84	134.86	
	4	413.25	404.53	376.32	
	5	503.77	500.35	487.58	
	6	571.19	566.72	549.03	
	1	32.503	31.846	29.675	
	2	128.91	127.94	123.95	
Mg Alloy	3	203.3	199.02	185.37	
	4	567.79	555.87	517.26	
	5	689.43	684.76	667.3	
	6	784.5	778.38	754.08	
	1	29.644	29.048	27.075	
	2	117.55	116.66	113.02	
Ti Alloy	3	185.41	181.53	169.13	
	4	517.85	507.04	471.96	
	5	626.32	622.08	606.24	
	6	715.21	709.65	687.51	
	1	32.887	32.217	30.005	
	2	130.7	129.5	125.47	
Al Alloy	3	205.7	201.33	187.42	
	4	574.49	562.32	522.96	
	5	703.12	698.35	680.49	
	6	794.37	788.13	763.53	

## Table 2: Comparison of Natural Frequency with and withoutcrack at 50 mm crack location

# Table 3: Comparison of Natural Frequency with and withoutcrack at 100 mm crack location

	100mm crack location				
Alloy	Natural Frequency (Hz)				
	Mode	without	2mm crack	4mm crack	
	Shape	crack	depth	depth	
	1	23.656	23.466	22.729	
	2	93.849	93.573	92.317	
Cu Alloy	3	147.97	146.63	138.87	
	4	413.25	409.23	390.112	
	5	503.77	504.62	498.01	
	6	571.19	569.27	556.93	
	1	32.503	32.243	31.233	
	2	128.91	128.54	126.81	
Mg Alloy	3	203.3	201.48	190.86	
	4	567.79	562.3	536.16	
	5	689.43	690.6	681.57	
	6	784.5	781.87	764.36	
	1	29.644	29.408	28.491	
Ti Alloy	2	117.55	117.2	115.63	
	3	185.41	183.76	174.12	
	4	517.85	512.88	489.4	
	5	626.32	627.39	619.19	
	6	715.21	712.82	696.86	
	1	32.887	32.621	31.592	
	2	130.7	130.11	128.37	
Al Alloy	3	205.7	203.84	193.01	
	4	574.49	568.88	542.2	
	5	703.12	704.31	695.07	
	6	794.37	790.169	773.97	

	150mm crack location						
	Natural Frequency (Hz)						
			2mm	4mm			
	Mode	without	crack	crack			
	Shape	crack	depth	depth			
	1	23.656	23.554	23.234			
	2	93.849	93.713	93.23			
Cu Alloy	3	147.97	147.09	143.63			
	4	413.25	409.89	398.27			
	5	503.77	503.67	502.53			
	6	571.19	569.99	564.46			
	1	32.503	32.363	31.925			
	2	128.91	128.73	128.07			
Mg Alloy	3	203.3	202.11	197.37			
	4	567.79	563.19	547.32			
	5	689.43	689.3	687.74			
	6	784.5	782.4	775.27			
	1	29.644	29.517	29.119			
	2	117.55	117.38	116.77			
Ti Alloy	3	185.41	184.33	180.04			
	4	517.85	513.68	499.28			
	5	626.32	626.2	624.79			
	6	715.21	713.7	706.81			
	1	32.887	32.744	32.297			
	2	130.7	130.31	129.64			
Al Alloy	3	205.7	204.48	199.64			
	4	574.49	569.8	553.56			
	5	703.12	702.98	701.38			
	6	794.37	792.69	785			

Table 4: Comparison of Natural Frequency with and withoutcrack at 150 mm crack location

 Table 5: Comparison of Natural frequency for without crack

	Natural Frequency Without						
	Crack						
Mode	Copper Mg Ti A						
Shape	Alloy	Alloy	Alloy	Alloy			
1	23.656	32.503	29.644	32.887			
2	93.849	128.91	117.55	130.7			
3	147.97	203.3	185.41	205.7			
4	413.25	567.79	517.85	574.49			
5	503.77	689.43	626.32	703.12			
6	571.19	784.5	715.21	794.37			

 Table 6: Comparison of Natural Frequency with different crack location at 2 mm crack depth

Crack	2mm crack depth           Natural Frequency (Hz)				
location					
	Mode	Cu	Mg	Ti	Al
	Shape	Alloy	Alloy	Alloy	Alloy
	1	23.176	31.846	29.048	32.217
	2	93.136	127.94	116.66	129.5
50mm	3	144.84	199.02	181.53	201.33
	4	404.53	555.87	507.04	562.32
	5	500.35	684.76	622.08	698.35
	6	566.72	778.38	709.65	788.13
100mm	1	23.466	32.243	29.408	32.621
	2	93.573	128.54	117.2	130.11
	3	146.63	201.48	183.76	203.84
	4	409.23	562.3	512.88	568.88
	5	504.62	690.6	627.39	704.31
	6	569.27	781.87	712.82	790.169
	1	23.554	32.363	29.517	32.744
	2	93.713	128.73	117.38	130.31
150mm	3	147.09	202.11	184.33	204.48
	4	409.89	563.19	513.68	569.8
	5	503.67	689.3	626.2	702.98
	6	569.99	782.4	713.7	792.69

It can be seen that in every mode shape Cu Alloy has minimum natural frequency while Al Alloy has maximum natural frequency. To reduce these natural frequencies cracks are introduced in different location with different crack depth and we analyzed that at 50 mm crack location with 4mm crack depth natural frequency has a minimum value for all alloys.

Now when frequency of alloys are compared with no crack and with 9 cracks then It has been observed that frequency decreases with number of cracks.

Table 7: Comparison of Natural Frequency with	h different
crack location at 4 mm crack depth	

Crack	4mm crack depth					
location	Natural Frequency					
	Mode	Cu	Mg	Ti	Al	
	Shape	Alloy	Alloy	Alloy	Alloy	
	1	21.59	29.675	27.075	30.005	
	2	90.233	123.95	113.02	125.47	
50mm	3	134.86	185.37	169.13	187.42	
	4	376.32	517.26	471.96	522.96	
	5	487.58	667.3	606.24	680.49	
	6	549.03	754.08	687.51	763.53	
	1	22.729	31.233	28.491	31.592	
	2	92.317	126.81	115.63	128.37	
100mm	3	138.87	190.86	174.12	193.01	
	4	390.112	536.16	489.4	542.2	
	5	498.01	681.57	619.19	695.07	
	6	556.93	764.36	696.86	773.97	
	1	23.234	31.925	29.119	32.297	
	2	93.23	128.07	116.77	129.64	
150mm	3	143.63	197.37	180.04	199.64	
	4	398.27	547.32	499.28	553.56	
	5	502.53	687.74	624.79	701.38	
	6	564.46	775.27	706.81	785	

## 3.1 Natural frequencies for various mode shapes

The modal analysis of the alloy beam is done on ANSYS 14. The following are the different mode shapes to produce natural frequency in composite beam



Figure 2 First mode of vibration



Figure 3 Second mode of vibration



Figure 4 Third mode of vibration



Figure 5 Forth mode of vibration



Figure 6 Fifth mode of vibration



Figure 7 Sixth mode of vibration

The first mode of vibration is a bending mode In this mode shape, the beam is tending to bend about the root section's The analysis shows that the parameter that effect root stiffness have a large impact on the first mode of frequency. The first mode frequency is also affected by parameters that effect tip mass.

The second mode of vibration is also a bending mode and the natural frequency of second mode of vibration is greater than the first mode of vibration.

The third mode of vibration is also bending mode with one node formation about the root, the frequency is more than the second mode .the deflection was in the vertical direction. The frequency is correspondingly higher due to increased stiffness in that direction.

The fourth mode of vibration is also bending mode with two node formation. The frequency of fourth mode shape is much higher than the above three modes.

The fifth mode of vibration is twisting about the root, the frequency is affected by tip rotational moment of inertia.

The frequency of sixth mode shape have the highest frequency in all the above mode shapes.

- Mode 1: When the force is applied at right angles to the surface of beam.
- Mode 2: When the force is applied vertically & horizontally on beam.
- Mode 3: Node formation during free vibrations due to forces at right angle to surface.
- Mode 4: Two node formation during free vibrations of the beam.
- Mode 5: Twisting of beam by fixing one end
- Mode 6: Natural vibration of the composite beam under transverse loading i.e. force acting along the width of beam.

## 4. Conclusion

The mechanical properties of aluminum alloy, magnesium alloy, titanium alloy and copper alloy were found by using computational method.

From the above results, following conclusions can be made

- Table 1 shows the comparison between the mechanical properties like tensile yield strength, tensile ultimate strength of all four alloys.
- From Figure-1 it can be concluded that the tensile strength of Ti alloy is highest amongst all alloys taken and has a minimum deflection comparison to all alloy
- The natural frequency decreases with increasing crack depth.
- From table 2-7 it has been observed that natural frequency decreases when number of cracks increases.

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